

**Table 9-1:** Properties of mixture in the ideal-gas state. All properties (mixture or pure component) are understood to be in the ideal-gas state. The superscripts <sup>ig</sup> and <sup>igm</sup> have been omitted for simplicity.

Property of ideal-gas mixture	Property of mixing	Partial molar
$V = \sum x_i V_i$	$\Delta V_{\text{mix}} = 0$	$\bar{V}_i = V_i$
$H = \sum x_i H_i$	$\Delta H_{\text{mix}} = 0$	$\bar{H}_i = H_i$
$S = \sum x_i S_i - R \sum x_i \ln x_i$	$\Delta S_{\text{mix}} = -R \sum x_i \ln x_i$	$\bar{S}_i = S_i - R x_i \ln x_i$
$U = \sum x_i U_i$	$\Delta U_{\text{mix}} = 0$	$\bar{U}_i = U_i$
$G = \sum x_i G_i + RT \sum x_i \ln x_i$	$\Delta G_{\text{mix}} = RT \sum x_i \ln x_i$	$\bar{G}_i = G_i + RT \ln x_i$

### Other Properties

Other properties of the ideal-gas mixture can be obtained easily. For example, for the internal energy we write

$$U^{\text{igm}} = H^{\text{igm}} - PV^{\text{igm}} = \sum_i x_i (H_i^{\text{ig}} - PV_i^{\text{ig}}),$$

where we used eqs. (9.26) and (9.25) for the enthalpy and volume of the ideal-gas mixture. The quantity in parenthesis on the right-hand side in the above equation is the ideal-gas internal energy. Therefore, the final result for internal energy is

$$U^{\text{igm}} = \sum_i x_i U_i^{\text{ig}}. \quad (9.32)$$

From this result it also follows that the internal energy of mixing is zero, and the partial molar internal energy is equal to the internal energy of the pure component:

$$\Delta U_{\text{mix}}^{\text{igm}} = 0, \quad (9.33)$$

$$\bar{U}_i = U_i. \quad (9.34)$$

The corresponding results for the Gibbs free energy are

$$G^{\text{igm}} = \sum_i x_i G_i^{\text{ig}} + RT \sum_i x_i \ln x_i, \quad (9.35)$$

$$\Delta G_{\text{mix}}^{\text{igm}} = RT \sum_i x_i \ln x_i, \quad (9.36)$$

$$\bar{G}_i = G_i + RT \ln x_i. \quad (9.37)$$

These are obtained from the relationship between  $G$ ,  $H$ , and  $S$  and their derivation is left as an exercise.

Right hand side missing xi  
before ln xi -- table 9-1  
has the right expression